



DEVELOPING NUMERICAL SIMULATIONS TO ASSIST IN ISOLATING EXCITED NITROUS OXIDE STATES

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Outline



INTRODUCTION

- Introduction
- Experimental
 - ▣ System Design
 - ▣ Results
- Computational Analysis
 - ▣ Motivation
 - ▣ Current Work
- Future Work



INTRODUCTION

Introduction

Overview



INTRODUCTION

- Purpose
 - Demonstrate dissociation of nitrous oxide with non-thermal plasma discharge
- Final objective
 - Achieve self-sustained dissociation using a dielectric barrier discharge (DBD)
 - Design and fabricate a hybrid electric/monopropellant thruster with this technology
- Nitrous oxide dissociation
 - **$\text{N}_2\text{O}(\text{g}) \rightarrow \text{N}_2(\text{g}) + \frac{1}{2}\text{O}_2(\text{g}) + \text{Heat}$**
 - 161 kJ/mol required to break apart N_2O
 - Oxygen molecules recombine and release 245 kJ/mol
 - Net energy ~ 84 kJ/mol
 - Self-sustained dissociation can be reached at high temperatures (>1000 °C)
- Benefits
 - “Greener” propellant than current monoprop’s (hydrazine, hydrogen peroxide)
 - Comparable specific impulse (~ 200 sec)
 - Non-toxic/non-flammable, safe to handle
 - Can be stored as a liquid

Past Research



INTRODUCTION

□ Previous Experiments

▣ Catalysts

- Reduce dissociation temperature
- Power only required at startup
- Material limitations
 - Not stable at high temperature

▣ Plasma

- Dissociation of NO_x
- Increased rate of decomposition
- 100% conversion achieved
- Continuous external power required

Hypothesis: Due to some of the gas being in an excited state, the effective activation energy for dissociation due to collisions may be reduced



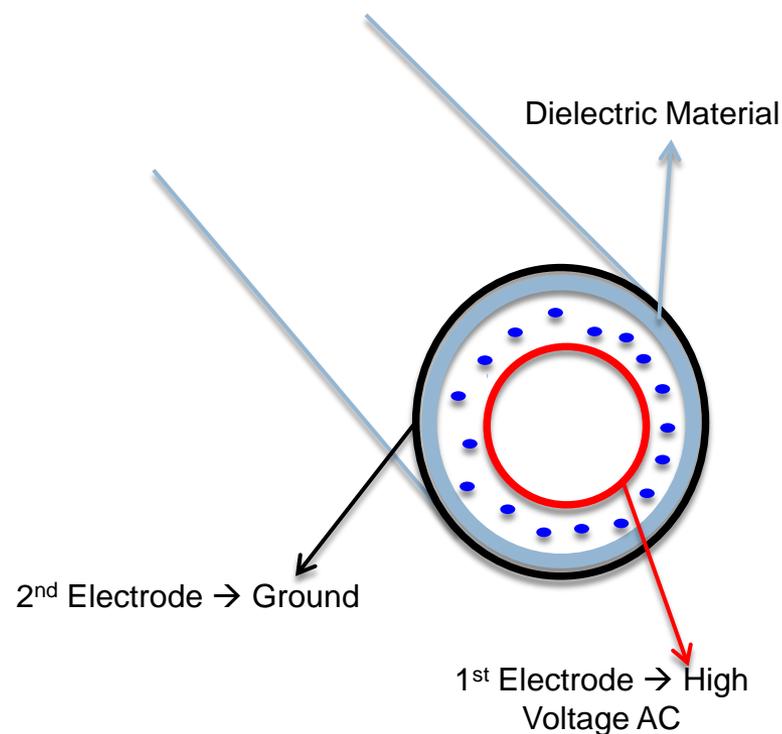
EXPERIMENTAL

Experimental: System Design

Dielectric Barrier Discharge

EXPERIMENTAL

- Dielectric Barrier Discharge (DBD)
 - ▣ Two concentric electrodes separated by an insulating dielectric barrier
 - ▣ High voltage AC
- Varying electric potential to accelerate free electrons
 - ▣ Electrons then collide with N_2O
 - ▣ Ions/additional free electrons formed
 - ▣ Trapped ions enhance collisionality
 - ▣ Only excitation and not full ionization may be sufficient
 - Reduction in activation energy predicted

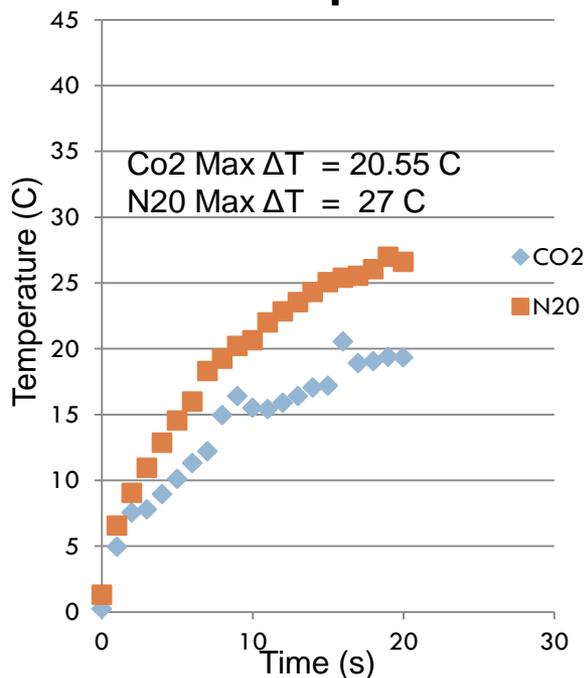


Proof of Concept Results

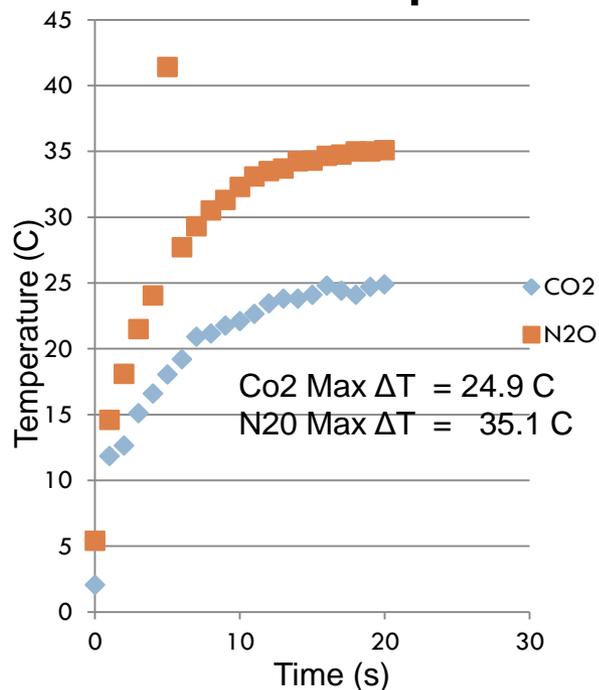
EXPERIMENTAL

- Tests using CO₂ as a control
- The specific heat for CO₂ is about 5% lower than N₂O.
 - This would result in CO₂ having a higher temperature increase (only joule heating)
 - However, we see the exact opposite

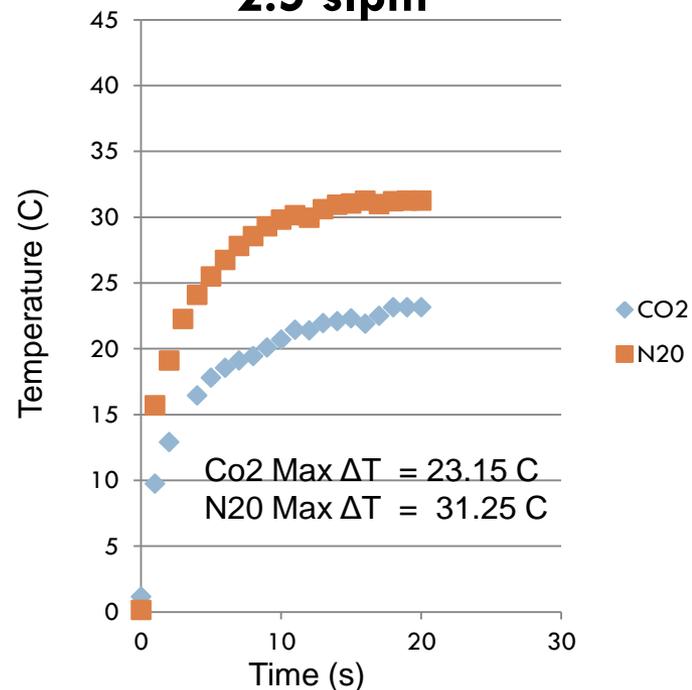
0.5 slpm



1.5 slpm

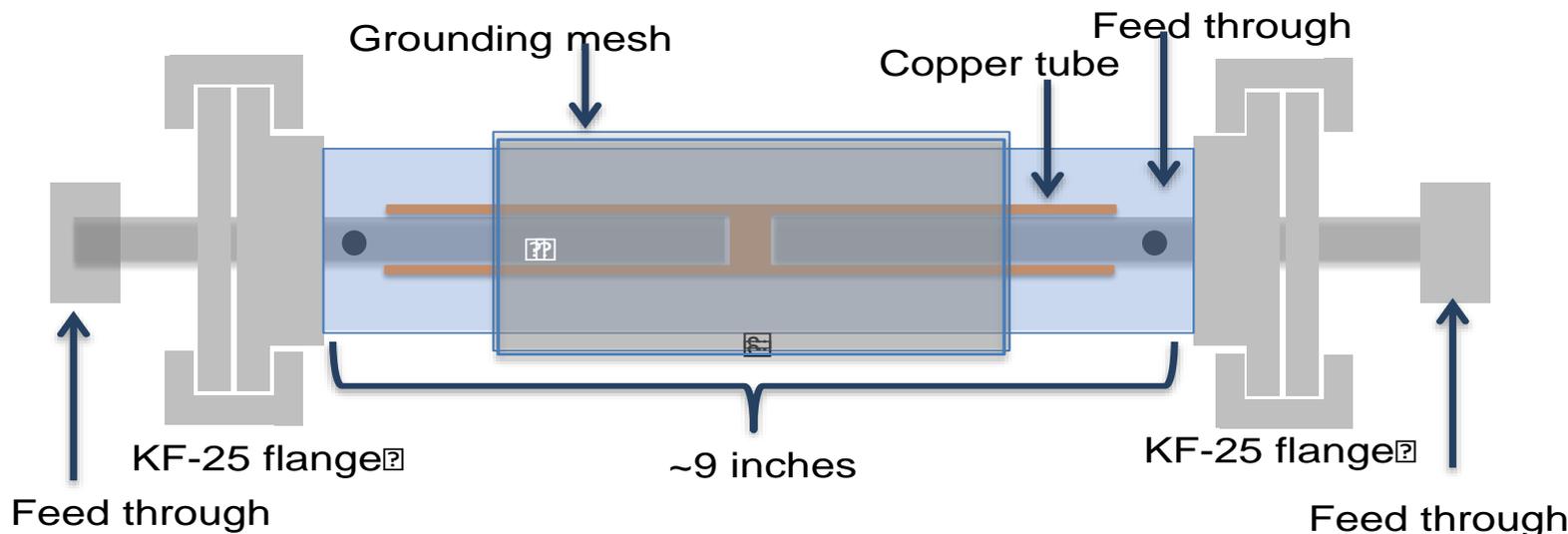


2.5 slpm



Current Design

EXPERIMENTAL

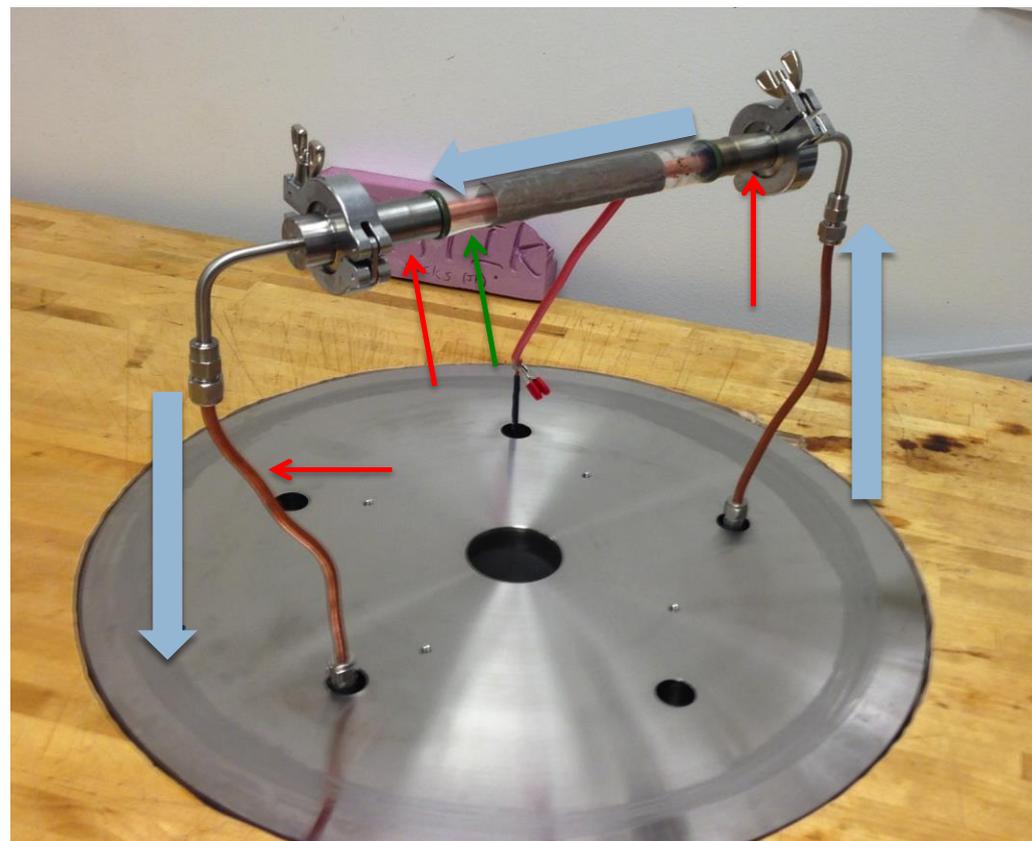


- Fused two stainless steel to quartz adapters (KF 25 Flanges)
- Placed in Bell Jar
 - ▣ Feed-throughs were connected to KF-25 ports on plate
 - ▣ Copper tube will “hold” the two feed-throughs
 - Direct flow out/in the holes in the feed-throughs
- Entire system grounded to grounding mesh

Bell Jar and Instrumentation

EXPERIMENTAL

- External flow meter
 - ▣ Switch between CO₂ and N₂O
 - ▣ Blue arrows show flow direction
- Thermocouples
 - ▣ Shown with red/green arrows
 - ▣ Red arrows are surface mounted to flanges and exit flow tube
 - ▣ Green arrow is internal to flow immediately downstream of plasma region
- Power input
 - ▣ *High voltage probe
 - ▣ *Series resistor to measure current



Reactor shown mounted on base plate without bell jar

*Some challenges still need to be addressed

Characterizing Power Loss

EXPERIMENTAL

- Power can be divided into the following:
 - ▣ Input power from plasma driver
 - Measured
 - ▣ Decomposition power
 - Unknown
 - ▣ Enthalpy increase of gas
 - Calculated using specific heats/tabulated values and measured temperatures
 - ▣ Radiative power loss
 - Inferred → will be baselined using CO₂

$$P_{input} + P_{decomp} - P_{rad} = P_{enthalpy}$$



EXPERIMENTAL

Experimental: Results

Results



EXPERIMENTAL

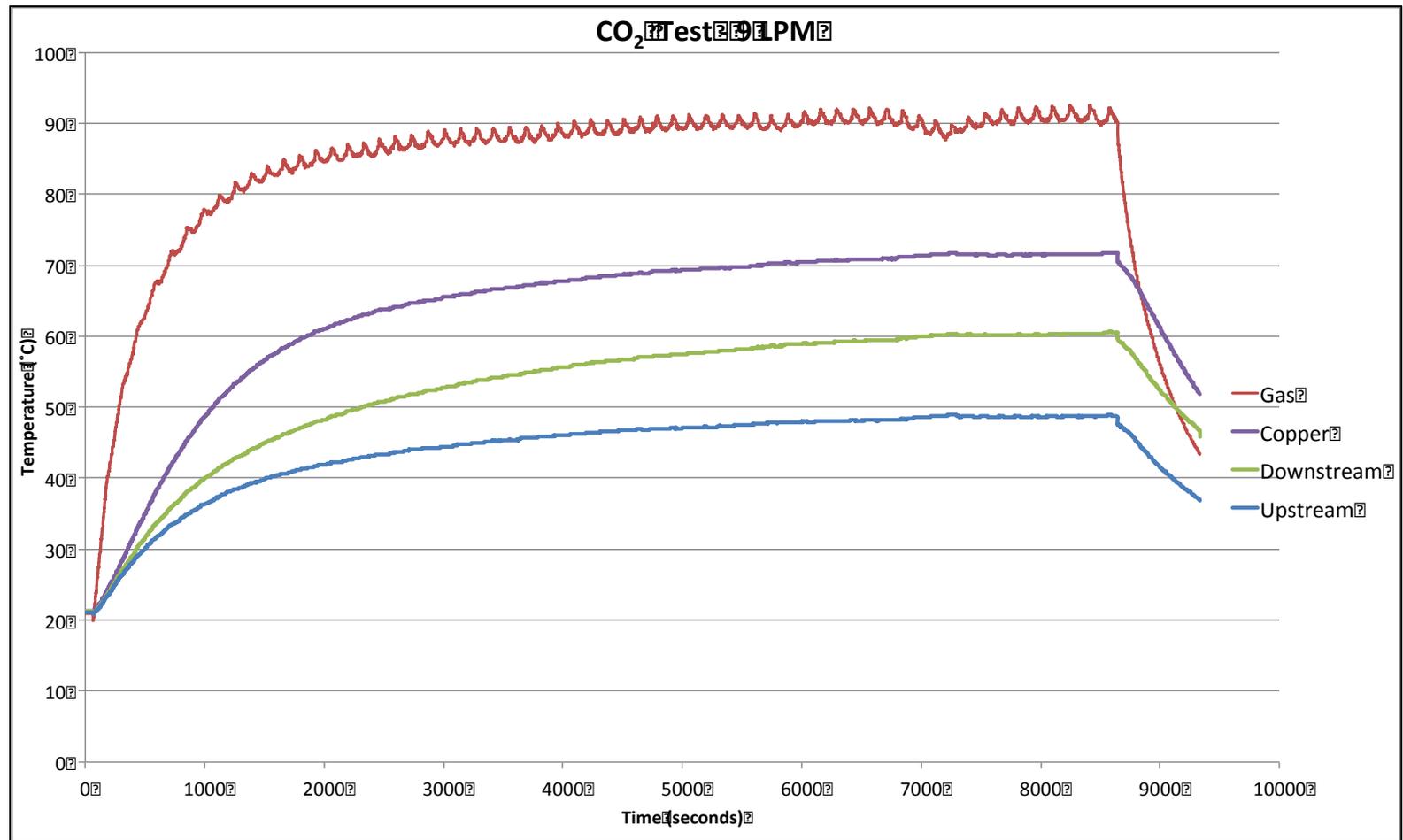
- Results with latest design
 - ▣ Gas flow at 9 LPM, ~30% maximum voltage
 - ▣ Run for about 2 hours to ensure steady-state
- Temperature data recorded from all four thermocouples
- Oscillation in gas temperatures
 - ▣ Period of ~2.5 min
 - ▣ Correlation to oscillation in the flow rate
 - ▣ Inverse relation shows higher temps at lower flow rates
 - Relationship is as expected, but cause of oscillation is currently unknown

CO₂ Temperature Data



EXPERIMENTAL

- Peak gas temperature around 90°C

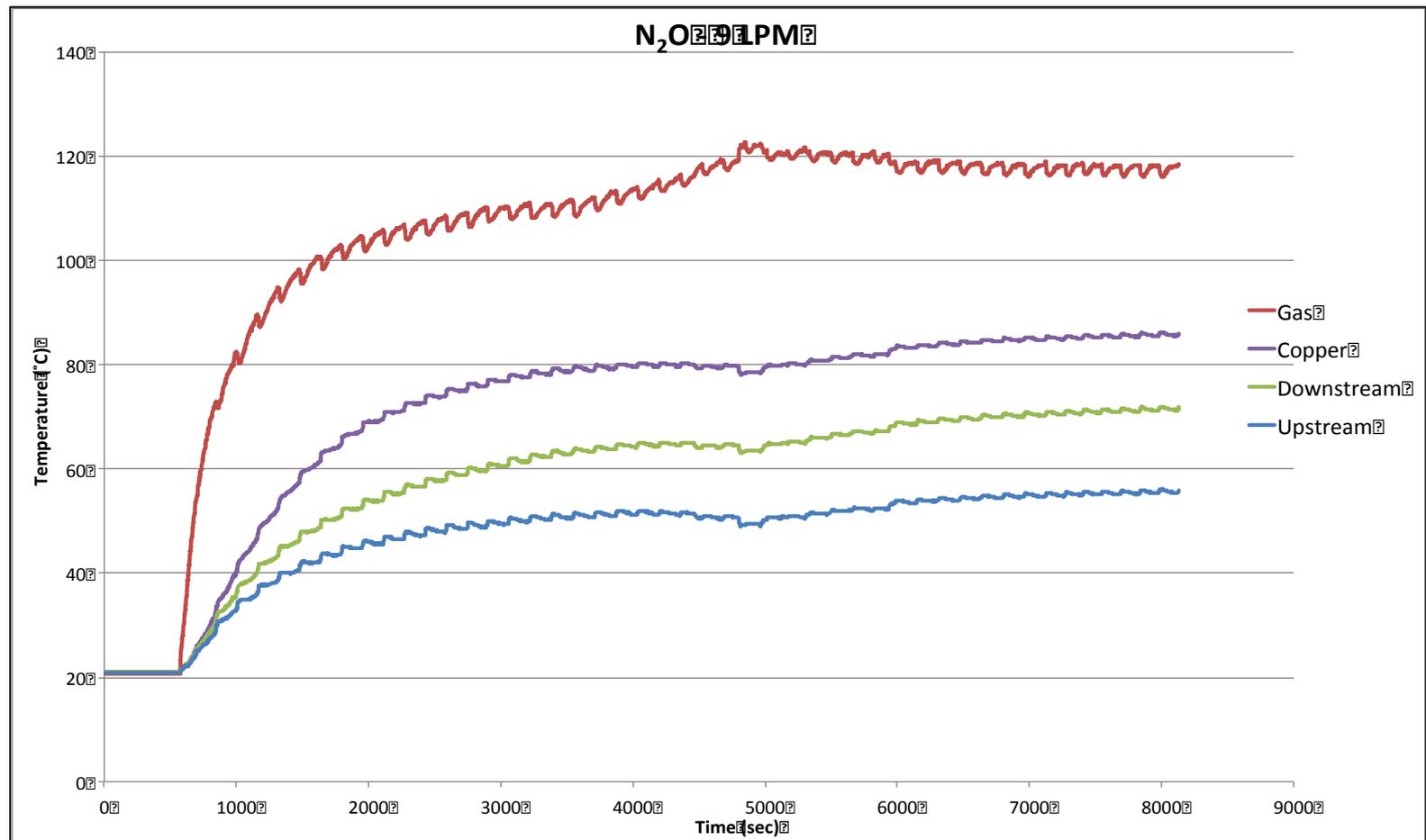


N₂O Temperature Data



EXPERIMENTAL

- Peak gas temperature around 120°C



Data Analysis: N₂O versus CO₂



EXPERIMENTAL

Location	% Power Increase
Power Supply	31
Gas (Enthalpy)	37
Copper (Rad)	17
Downstream (Rad)	15
Upstream (Rad)	7

6% difference

- Graphs show temperature is higher (30°C) for N₂O
- ~31% more power into the N₂O from the power supply
 - ▣ Characteristic of ionization/excitation energies and cross-sections
- Radiated power increase shown above at each thermocouple location
- Conclusion
 - ▣ Net power released through decomposition of N₂O
 - ▣ Presence of plasma is either:
 - Reducing activation energy (low energy cost – desirable) or
 - Directly dissociating N₂O (high energy cost – not desirable)



COMPUTATIONAL

Computational Analysis: Motivation

Isolating Excited States of N₂O

COMPUTATIONAL

- ▣ External power required to dissociate N₂O is deemed excessive
 - High energy cost – not desirable
- ▣ Hypothesis:
 - Due to some of the gas being in an excited state, the effective activation energy for dissociation due to collisions may be reduced
- ▣ Ionization energy for N₂O – electrons accelerated in DBD
 - ~12.9 eV
- ▣ Goal: Input energy less than that to minimize the amount of power required

Dissociation Paths

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- Possible dissociation paths with energies less than ~ 13 eV
 - 7.8 eV
 - 8.5 eV
 - 9.6 eV
- Build/design an electron source
 - Accelerate electrons to certain energy levels
 - Collide with neutral gas, induce excitation



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Computational Analysis: Current Work

Numerical Model



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- A 2-D numerical model will provide a guideline for experimentation
- First step → 1-D model of plasma within a chamber
 - ▣ Implement “extractor grids” to accelerate electrons
- Simulation (1-D):
 - ▣ Fluid treatment for ions and electrons
 - ▣ Transport model: Drift Diffusion
 - Drift – electric field, Diffusion – gradient of density, temperature

Scharfetter-Gummel (SG) Method



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- Method used to discretize the drift-diffusion equations
- Species density evaluated on cell centers (i)
 - ▣ All other quantities evaluated on cell boundaries ($i \pm 1/2$)
- Fluxes approximated across the cell
 - ▣ All variables constant other than density
 - ▣ First order differential equation in density
 - ▣ Provides more stability

Equations (1)

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Electrons

$$\frac{\partial n_e}{\partial t} + \nabla \cdot \Gamma_e = S_e$$

$$\Gamma_e = -\mu_e E n_e - \mu_e T_e \nabla n_e - k_t \mu_e n_e \nabla T_e$$

Ions

$$\frac{\partial n_i}{\partial t} + \nabla \cdot \Gamma_i = S_i$$

$$\Gamma_i = \mu_i E n_i - \mu_i T_i \nabla n_i$$

Assuming all values other than density constant...

General form of fluxes:

$$\Gamma_{i+\frac{1}{2}} = \sigma \left(\frac{\lambda}{e^{\lambda dx} - 1} n_{i+1} + \frac{\lambda}{e^{-\lambda dx} - 1} n_i \right)$$

Note density dependence from adjacent nodes!

Equations (2)

COMPUTATIONAL

Electron Sources*

Ion Sources*

$$S_e = \alpha |\Gamma_e| - \beta n_e n_i - \nu_a n^2 n_e$$

Ionization

Recombination

3 - Body

$$S_i = \alpha |\Gamma_e| - \beta n_e n_i$$

Ionization

Recombination

- Semi-implicit time-stepping method
 - Allows for larger time-steps
 - Lower computation time

$$\frac{n_i^k - n_i^{k-1}}{\Delta t} + \frac{\Gamma_{i+\frac{1}{2}} - \Gamma_{i-\frac{1}{2}}}{\Delta x} = S$$

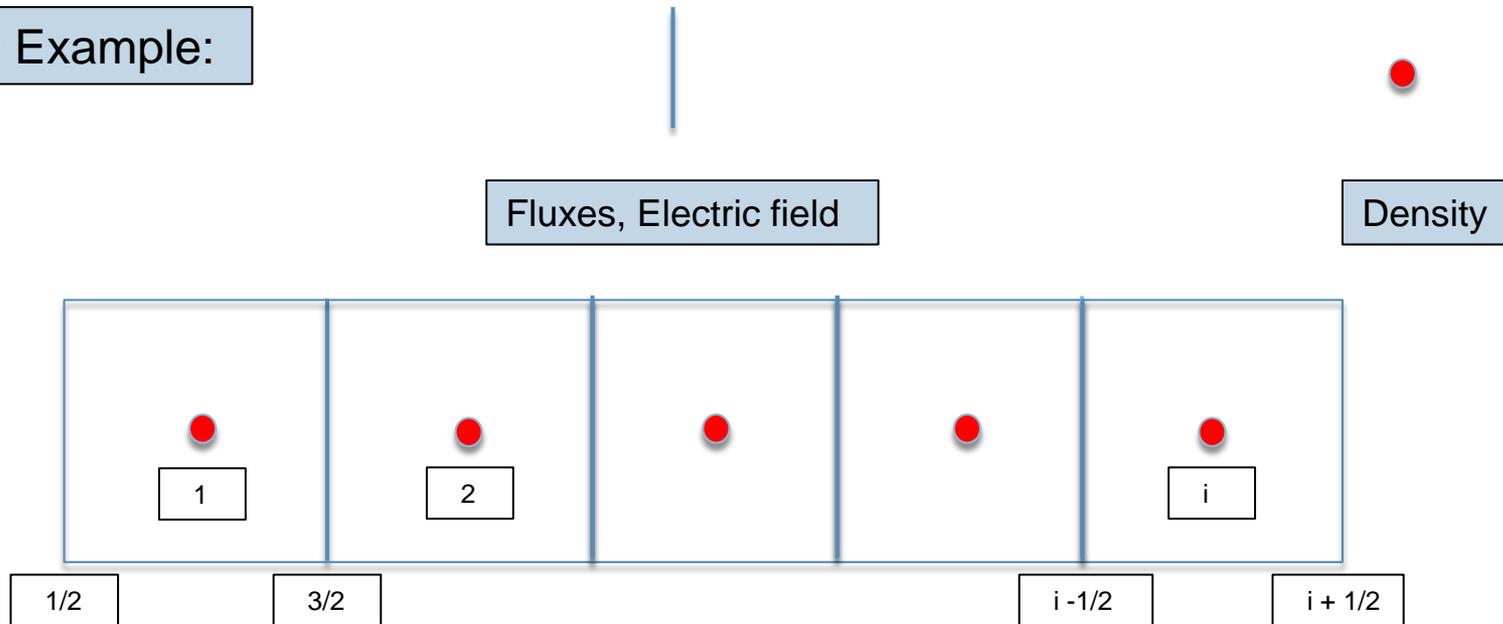
$$\Gamma = \Gamma(n^k, \Phi^{k-1})$$

*Ignored negative ions

Mesh

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1-D Example:



SG assumes all variables other than density constant across a cell i
- calculated on the boundaries of the cells

Wall Boundary Conditions

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- Boundary conditions applied on flux nodes
 - ▣ Somewhat difficult to find ones that made sense physically and numerically
- Current BC:
 - ▣ Assuming small gradients of temperature & density
 - ▣ Up-wind scheme → assume fluxes always going into the wall
 - Unsure about this condition but presents the best results

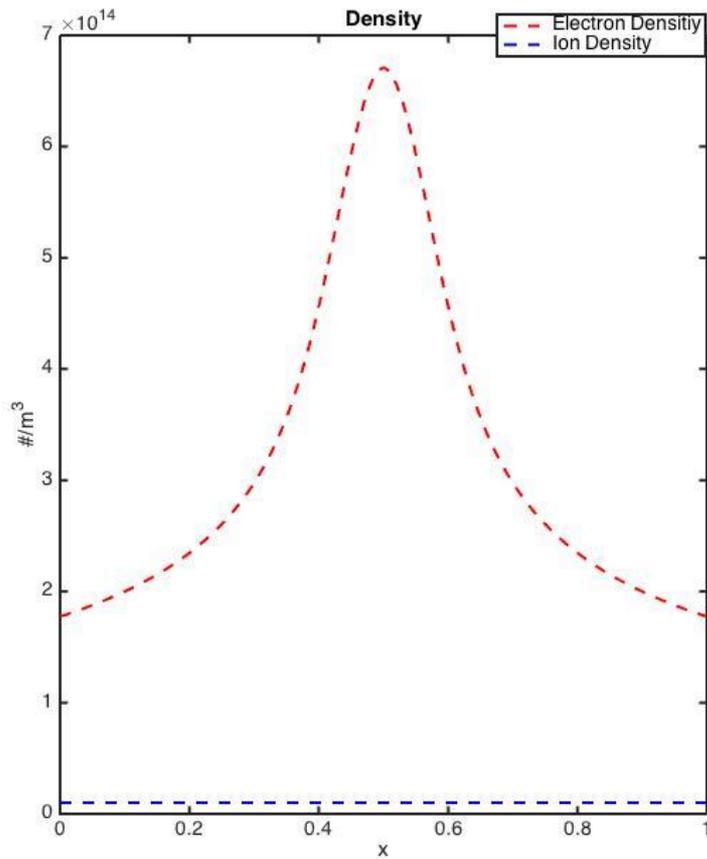
$$n_1^k + \frac{\Delta t}{\Delta x} [(a\mu En_e)_1 + (b\mu En_e)_2] = S + n_1^{k-1} \quad \leftarrow \quad \boxed{\text{Left Boundary}}$$

$$\boxed{\text{Right Boundary}} \quad \longrightarrow \quad n_x^k + \frac{\Delta t}{\Delta x} [(a\mu En_e)_x + (b\mu En_e)_{x-1}] = S + n_x^{k-1}$$

a and b → coefficients to ensure upwind towards boundaries

Electrons – Gaussian Source

COMPUTATIONAL



Time(22) - 1.1171e-07 seconds
End Time - 0.005 sec

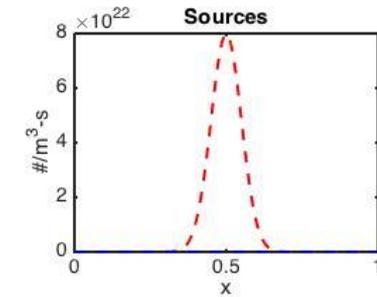
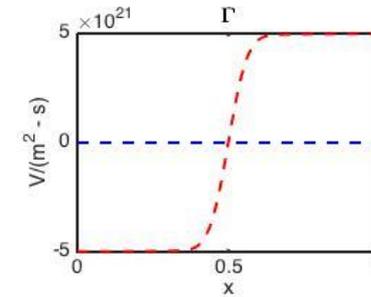
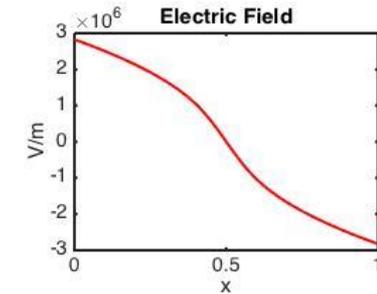
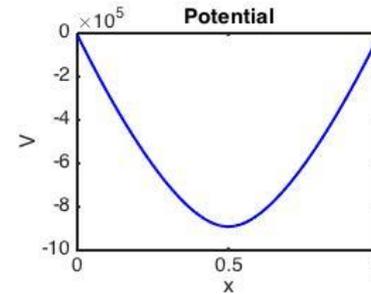
SYSTEM STATUS

$\Delta x = 1 \text{ m}$
CFL - 1
 $\Delta t = 1 \text{ seconds}$
of Segments - 201
Boundary Conditions - Flux
Ion initial density - 100000000000000 $\#/\text{m}^3$
Electron initial density - 0 $\#/\text{m}^3$

SIMULATION

Te - 3 eV, Ti - 0.025875 eV
 $\mu(-) - 9.9501 \text{ m}^2/\text{V}\cdot\text{s}$, $\mu(+)$ - 0.023453 $\text{m}^2/\text{V}\cdot\text{s}$

Max α value - 253707.7792, at 1.005 m
Max β value - 9.5342e-08, at 0.505 m
Max kd value - 0, at 0.005 m
Max ν value - 1.8162e-06, at 0.505 m



Extractor Plates

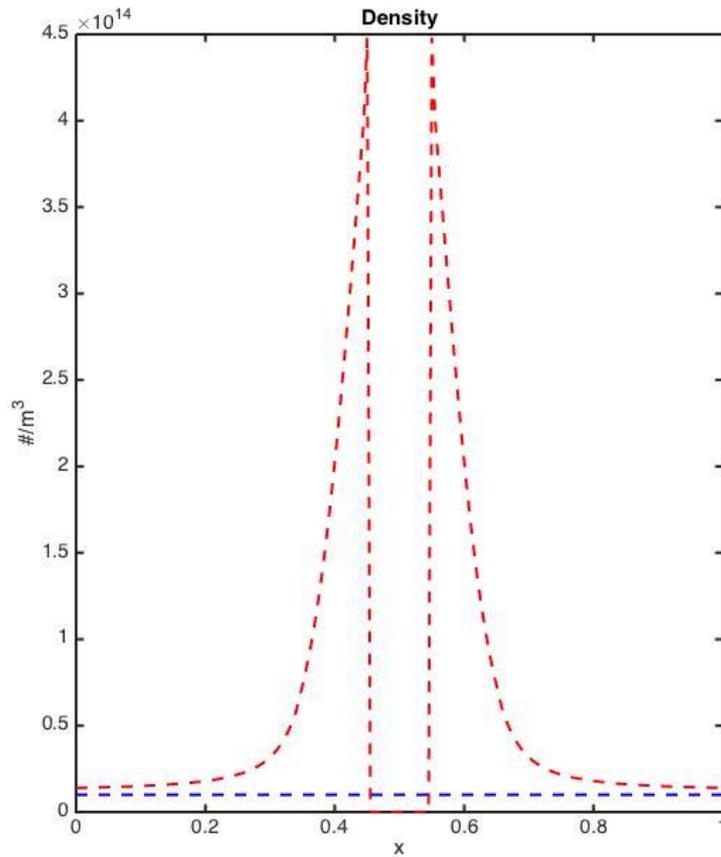


COMPUTATIONAL

- Extractor plates required to accelerate electrons
- 1-D simulation
 - ▣ Imposed potential on a plate in the middle
 - ▣ Wall boundaries on plate edges
- In 2-D simulation
 - ▣ Used to extract electrons and accelerate to desired energy levels

Electrons – Gaussian Source + Emitter

COMPUTATIONAL



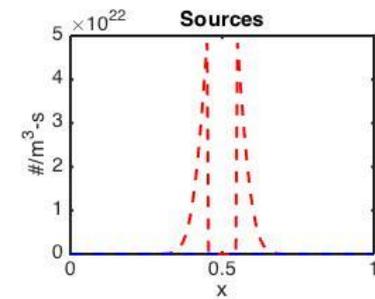
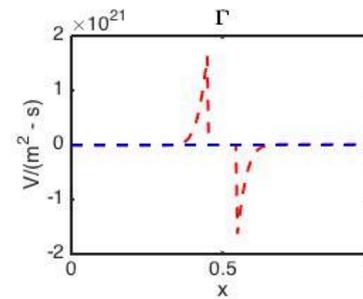
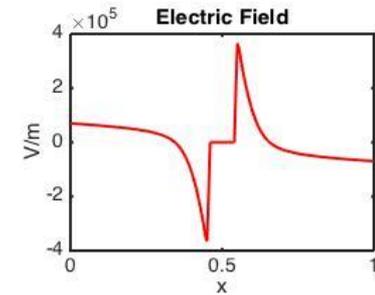
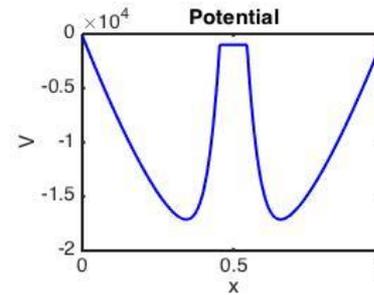
Time(142) - 7.2101e-07 seconds
End Time - 0.005 sec

SYSTEM STATUS

$\Delta x = 1$ m
CFL - 1
 $\Delta t = 1$ seconds
of Segments - 201
Boundary Conditions - Flux
Ion initial density - 10000000000000 #/m³
Electron initial density - 0 #/m³

SIMULATION

Te - 3 eV, Ti - 0.025875 eV
 $\mu(-) - 9.9501$ m²/V-s, $\mu(+)$ - 0.023453 m²/V-s
Max α value - 10755.9985, at 0.455 m
Max β value - 6.3669e-08, at 0.555 m
Max kd value - 0, at 0.005 m
Max ν value - 1.2129e-06, at 0.555 m





FUTURE WORK

Future Work



Future Work



FUTURE WORK

- Numerical Analysis
 - Implement sources/sinks into model
 - Ionization/recombination coefficients
 - Boundary conditions
 - Extend to 2-D
 - Extractors
 - Control electron energy levels
 - Model collisions with N_2O
- Experimental setup
 - Design electron source
 - Isolate excited states of nitrous oxide
- Main goal: Achieve self-sustained decomposition

References



FUTURE WORK

- ¹Zakirov, V.A., Goeman, V., Lawrence, T.J., Sweeting, M.M. "Nitrous Oxide Catalytic Decomposition for Space Applications," Surrey Space Center, AIAA 2001-3922 (2001)
- ²Zakirov, Vadim. "Nitrous Oxide as a Rocket Propellant." *Acta Astronautica* 48.5-12 (2001): 353-62. Print.
- ³Mclarnon, C.R., Mathur, V.K., "Nitrogen Oxide Decomposition by Barrier Discharge," *Industrial & Engineering Chemistry Research*, Vol. 39, No. 8, pp. 2779-2787 (2000)
- ⁴Steitz, David E. "NASA - National Aeronautics and Space Administration." NASA. N.p., 15 Aug. 2012. Web. 03 Dec. 2012. <http://www.nasa.gov/home/hqnews/2012/aug/HQ_12-281_Green_Propellants.html>.
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- ⁶Recktenwald Gerald W. "Finite-Difference Approximations to the Heat Equation." THS, Royal Institute of Technology, 6 Mar. 2011. Web. <<http://www.f.kth.se/~jgalap/numme/FDheat.pdf>>.
- ⁷Plasma-Assisted Combustion of N₂O/Ethanol Propellant for Space Propulsion, Akira Kakami, Taku Egawa, Natsuki Yamamoto, and Takeshi Tachibana. 46th AIAA/ASME/SAE/ASEE Joint Propulsion Conference & Exhibit. July
- ⁸Wallbank, J., P. Sermon, A. Baker, K. Courtney, and R. Sambrook. "Nitrous Oxide as a Green Monopropellant for Small Satellites." *ESA Special Publication 557* (2004): n. pag. Web. <<http://adsabs.harvard.edu/abs/2004ESASP.557E..20W>>
- ⁹Vadim Zakirov, Hai-yun Zhang, A model for the operation of nitrous oxide monopropellant, *Aerospace Science and Technology*, Volume 12, Issue 4, June 2008, Pages 318-323, ISSN 1270-9638, <http://dx.doi.org/10.1016/j.ast.2007.08.003>. (<http://www.sciencedirect.com/science/article/pii/S1270963807001046>)
- ¹⁰Kogelschatz, U. "Fundamentals and Applications of Dielectric-Barrier Discharges." N.p., 24 May 2000. Web.



FUTURE WORK

Questions?

